

Mark Scheme (Results) Summer 2007

GCE

GCE Mathematics

Statistics S2 (6684)

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June 2007 6684 Statistics S2 Mark Scheme

Question Number	Scheme	Marks
1(a)	Continuous uniform distribution or rectangular distribution.	B1
	$f(x)$ $\frac{1}{5}$ 0 may be implied by start at y axis	B1
	$0 \qquad 5 \qquad x \qquad$	B1 (3)
(b)	E(X) = 2.5 ft from their a and b, must be a number	B1ft
	$Var(X) = \frac{1}{12}(5-0)^2 \qquad \text{or attempt to use } \int_0^5 f(x)x^2 dx - \mu^2 \qquad \text{use their } f(x)$	M1
	$=\frac{25}{12}$ or 2.08 o.e awrt 2.08	A1
		(3)
(C)	$P(X > 3) = \frac{2}{5} = 0.4$ 2 times their 1/5 from diagram	B1ft (1)
(d)	P(X=3)=0	B1 (1)
		(Total 8)

Question Number		Scheme		Marks
2	$\frac{\text{One tail test}}{\text{Method 1}}$ $H_{o}: \lambda = 5 \ (\lambda = 2.5)$ μ $H_{1}: \lambda > 5 \ (\lambda > 2.5)$		may use λ or	B1 B1 M1
	$X \sim \text{Po} (2.5)$ P($X \ge 7$) = 1 - P($X \le 6$) = 1 - 0.9858	$[P(X \ge 5) = 1 - 0.8912 = 0.1088]$ $P(X \ge 6) = 1 - 0.9580 = 0.0420$	may be implied att $P(X \ge 7) P(X \ge 6)$	M1
	= 0.0142	$\operatorname{CR} X \ge 6$	awrt 0.0142	Al Ml
	0.0142 < 0.05 (Reject H ₀ .) There is signific	$7 \ge 6$ or 7 is in critical region or 7 is cant evidence at the 5% significance 1	significant evel that the factory	B1
-	is polluting the river with ba or The scientists claim is justifi	cteria.		(7) Total 7
	$\frac{\text{Method } 2}{\text{H}_{\text{o}}: \lambda = 5} (\lambda = 2.5)$ $\text{H}_{1}: \lambda > 5 (\lambda > 2.5)$		may use λ or μ	B1 B1
	<i>X</i> ~ Po (2.5)		may be implied	MI
	P(X < 7)	[P(X < 5) = 0.8912] P(X < 6) = 0.9580	att P(X < 7) $P(X < 6)$	
	= 0.9858	$\operatorname{CR} X \ge 6$	wrt 0.986	M1 A1
	0.9858 > 0.95	$7 \ge 6$ or 7 is in critical region or 7 is	significant	MI D1
	(Reject H ₀ .) There is signific is polluting the river with ba <u>or</u> The acienticta claim is justifi	cant evidence at the 5% significance l cteria.	evel that the factory	(7)
	The scientists claim is justifi	ea		

Two tail test Method 1			
<u></u>		B1	
$H_{o}: \lambda = 5 \ (\lambda = 2.5)$	may use λ or μ	B0	
$H_1: \lambda \neq 5 \ (\lambda \neq 2.5)$		M1	
<i>X</i> ~ Po (2.5)			
$P(X \ge 7) = 1 - P(X \le 6)$	$\begin{bmatrix} P(X \ge 6) = 1 - 0.9580 = 0.0420 \end{bmatrix} \text{ att } P(X \ge 7) P(X \ge 7)$	M1	
- 1 - 0.9838	$P(X \ge 7) - 1 - 0.9838 - 0.0142$	A 1	
= 0.0142	$CR X \ge 7 \qquad awrt \ 0.0142$	AI	
0.0142 < 0.025	$7 \ge 7$ or 7 is in critical region or 7 is significant	M1	
(Deinst II.) There is similar		B1	
is polluting the river with b	acteria.		
or The second se			
The scientists claim is justif	fied		
Mathad 2		R1	_
$\frac{1}{H_0} : \lambda = 5 \ (\lambda = 2.5)$	may use λ or μ	BO	
$H_1: \lambda \neq 5 \ (\lambda \neq 2.5)$		N/1	
<i>X</i> ~ Po (2.5)		1 VI 1	
P(X < 7)	$\begin{bmatrix} P(X < 6) = 0.9580 \end{bmatrix} \text{ att } P(X < 7) = 0.9858$		
		M1A1	
= 0.9858	$\operatorname{CR} X \ge 7 \qquad \operatorname{awrt} 0.986$	1.01	
0.9858 > 0.975	$7 \ge 7$ or 7 is in critical region or 7 is significant	MI	
(Reject H.) There is signif	I	B1	
is polluting the river with b	acteria <u>.</u>		
<u>or</u> The asigntists shi	Gad		
i ne scientists claim is justi	nea		

Question Number	Scheme		Marks
3(a)	$X \sim Po(1.5)$ need Po and 1.5	B1	(1)
(b)	Faulty components occur at a constant rate.any two of the 3Faulty components occur independently or randomly.only need faultyFaulty components occur singly.once	B1 B1	(2)
(C)	$P(X=2) = P(X \le 2) - P(X \le 1)$ or $\frac{e^{-1.5}(1.5)^2}{2}$	M1	
	= 0.8088 - 0.5578		
	= 0.251 awrt 0.251	A1	
			(2)
(d)	$X \sim Po(4.5)$ 4.5 may be implied	B1	
	$P(X \ge 1) = 1 - P(X = 0)$ = 1 - e^{-4.5}	M1	
	= 1 - 0.0111 = 0.9889 awrt 0.989	A1	(3)
			Total 8

Question Number	Scheme		
4	Attempt to write down combinationsat least one seen $(5, 5, 5)$ $(5, 5, 10)$ and order $(10, 10, 5)$ and order $(10, 10, 10)$	M1 A1	
	(5,5,5), (10,5,5), (10,5,10), (5,10,10), (5,10,5), (10,5,5), (10,5,10), (5,10,10), (5,10,5), (10,5,5), (10,5,10), (5,10,10), (5,10,5), (10,5,5), (10,5,10), (5,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,10,10), (10,5,5), (10,5,5), (10,5,10), (10,5,5), (10,5,5), (10,5,10), (10,5,5), (10,5,5), (10,5,10), (10,5,5), (10,5,5), (10,5,10), (5,10,10), (10,10,10), (10,5,10), (10,5,5), (10,5,10), (5,10,10), (10,5,10), (10,5,10), (5,10,10), (10,5,10), (10,5,10), (5,10,10), (10,5,10), (10,5,10), (5,10,10), (10,5,10),	A1	
	median 5 and 10 Median = 5 $P(M = m) = \left(\frac{1}{4}\right)^3 + 3\left(\frac{1}{4}\right)^2 \left(\frac{3}{4}\right) = \frac{10}{64} = 0.15625$ add at least two prob using ¹ / ₄ and ³ / ₄ . identified by having same median of 5 or 10 Allow no 3 for M	B1 M1 A1	
	Median = 10 P(M = m) = $\left(\frac{3}{4}\right)^3 + 3\left(\frac{3}{4}\right)^2 \left(\frac{1}{4}\right) = \frac{54}{64} = 0.84375$	A1 (7) Total 7	

Question Number	Scheme			Marks	
5(a)	If $X \sim B(n,p)$ and n is large, $n > 50p$ is small, $p < 0.2then X can be approximated by Po(np)$		B1 B1	(2)	
(b)	P(2 consecutive calls) = 0.01^2 = 0.0001		M1 A1	(2)	
(c)	<i>X</i> ~B(5, 0.01)	may be implied	B1		
	P(X > 1) = 1 - P(X = 1) - P(X = 0) = 1 - 5(0.01)(0.99) ⁴ - (0.99) ⁵ = 1 - 0.0480298 - 0.95099		M1		
	= 0.00098	awrt 0.00098	A1	(3)	
(d)	$X \sim B(1000, 0.01)$ Mean = $np = 10$ Variance = $np(1 - p) = 9.9$	may be implied by correct mean and variance	B1 B1 B1	(3)	
(e)	$X \sim \text{Po}(10)$				
	$P(X > 6) = 1 - P (X \le 6)$ = 1 - 0.1301 = 0.8699	awrt 0.870	M1 A1		
				(2)	
				Total 12	

Question Number		Scheme		Marks
6	$\label{eq:constraint} \begin{array}{l} \underline{\text{One tail test}} \\ \underline{\text{Method 1}} \\ H_{\text{o}}: p = 0.2 \\ H_{1}: p > 0.2 \end{array}$			B1 B1
	$X \sim B(5, 0.2)$	may	be implied	M1
	$P(X \ge 3) = 1 - P(X \le 2)$ = 1 - 0.9421	$\begin{bmatrix} P(X \ge 3) = 1 - 0.9421 = 0.0579 \\ P(X \ge 4) = 1 - 0.9933 = 0.0067 \end{bmatrix}$	att P($X \ge 3$) P($X \ge 4$)	M1
	= 0.0579	$\operatorname{CR} X \ge 4$	awrt 0.0579	A1
	0.0579 > 0.05	$3 \le 4$ or 3 is not in critical region of	r 3 is not significant	M1
-	(Do not reject H ₀ .) There is in there is an increase in the nu Or Linda's claim is not justi	insufficient evidence at the 5% signi umber of times the taxi/driver is late. ified	ficance level that	B1 (7) Total 7
	$\label{eq:method_linear} \begin{array}{l} \underline{\text{Method 2}} \\ H_{o}: p = 0.2 \\ H_{1}: p > 0.2 \end{array}$			B1 B1
	$X \sim B(5, 0.2)$	may	be implied	M1
	P(X < 3) =	[P(X < 3) = 0.9421] P(X < 4) = 0.9933	att P(X < 3) $P(X < 4)$	
	0.9421	$\operatorname{CR} X \ge 4$	awrt 0.942	M1A1
	0.9421 < 0.95	$3 \le 4$ or 3 is not in critical region or	3 is not significant	M1
	(Do not reject H ₀ .) There is in there is an increase in the nu Or Linda's claim is not justi	insufficient evidence at the 5% signi umber of times the <u>taxi/driver is late.</u> ified	ficance level that	B1 (7)

<u>Two tail test</u> Method 1			B1	
$\frac{H}{H_o: p = 0.2}$			B0	
$H_1: p \neq 0.2$			M1	
$X \sim X \sim B(5, 0.2)$	1	may be implied	M1	
$P(X \ge 3) = 1 - P(X \le 2)$	$[P(X \ge 3) = 1 - 0.9421 = 0.0579]$	att P($X \ge 3$) P($X \ge 4$)	1411	
= 1 - 0.9421	$P(X \ge 4) = 1 - 0.9933 = 0.0067$		A1	
= 0.0579	$\operatorname{CR} X \ge 4$	awrt 0.0579	M1	
0.0579 > 0.025	$3 \le 4$ or 3 is not in critical region or 3	3 is not significant	D1	
(Do not reject $H_{0.}$) There is in there is an increase in the nu Or Linda's claim is not justi	insufficient evidence at the 5% signifing the signification of times the taxi/driver is late. fied	icance level that	BI	(7)
			B1	
$\frac{\text{Method } 2}{\text{H}_0: p = 0.2}$			B0	
$H_1: p \neq 0.2$			M1	
$X \sim X \sim B(5, 0.2)$	I	may be implied		
P(X < 3) =	[P(X < 3) = 0.9421] P(X < 4) = 0.9933	att P($X < 3$) P($X < 4$)		
0.9421	$\operatorname{CR} X \ge 4$	awrt 0.942	M1A1	
0.9421 < 0.975	$3 \le 4$ or 3 is not in critical region or	3 is not significant	M1	
Do not reject H ₀ . There is in there is an increase in the nu Or Linda's claim is not justi	sufficient evidence at the 5% signification mber of times the taxi/driver is late. fied	ance level that	B1	(7)
Special Case				
If they use a probability of	$\frac{1}{7}$ throughout the question they may g	gain B1 B1 M0 M1		
A0 M1 B1.	1			
NB they must attempt to wo	ork out the probabilities using $\frac{1}{7}$			
	I I			

Question Number	Scheme	
7(a) i ii	If $X \sim B(n,p)$ and n is large or $n > 10$ or $np > 5$ or $nq > 5p$ is close to 0.5 or $nq > 5$ and $np > 5then X can be approximated by N(np,np(1-p))mean = npvariance = np(1-p)must be in terms of p$	B1 B1 (2) B1 B1
		(2)
(b)	$X \sim N (60, 58.2) \text{ or } X \sim N (60, 7.63^2) $ $P(X \ge 40) = P(X > 39.5) $ $((20.5 + 60)) $ $((20.5 + 60)) $ $((20.5 + 60)) $	B1, B1 M1
	$= 1 - P\left(z < \pm \left(\frac{39.5 - 60}{\sqrt{58.2}}\right)\right)$ standardising 39.5 or 40 or 40.5 and their µ and σ = 1 - P(z < -2.68715)	M1
	= 0.9965 allow answers in range 0.996 – 0.997	A1dep on both M
(c)	E(X) = 60 may be implied or ft from part (b)	(5) B1ft
	Expected profit = $(2000 - 60) \times 11 - 2000 \times 0.70$ = £19 940.	M1 A1 (3) Total 12

