

GCSE MATHEMATICS 8300/1H

Higher Tier Paper 1 Non-Calculator

Mark scheme

November 2018

Version: 1.0. Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Question	Answer	Mark	Comments
1	5 ⁸	B1	
2	200π	B1	
3	22 <i>a</i>	B1	
		-	
4	$\frac{\sqrt{3}}{2}$	B1	

Question	Answer	Mark	Comments	
	Alternative method 1			
	$\frac{17}{2}$ or $\frac{8}{3}$	M1	oe fractions	
	their $\frac{17}{2}$ × their $\frac{3}{8}$	M1	conversion of both mixed numbers to improper fractions and multiplication of the conversion of $8\frac{1}{2}$ by the reciprocal of the conversion of $2\frac{2}{3}$	
	<u>51</u> 16	A1	oe fraction or decimal	
	$3\frac{3}{16}$	B1ft	oe mixed number ft correct conversion of their improper fraction to a mixed number	
5	Alternative method 2			
	$\frac{17}{2}$ or $\frac{8}{3}$	M1	oe fractions	
	$\frac{51}{6} \div \frac{16}{6}$	M1	conversion of both mixed numbers to improper fractions, correct conversion to improper fractions with a common denominator and division of the conversion of $8\frac{1}{2}$ by the conversion of $2\frac{2}{3}$	
	<u>51</u> 16	A1	oe fraction or decimal	
	$3\frac{3}{16}$	B1ft	oe mixed number ft correct conversion of their improper fraction to a mixed number	

The Additional Guidance for question 5 is on the next page

Question	Answer	Mark	Comme	nts			
	Additional Guidance						
	Working with decimals			0, 3 or 4			
	Ignore incorrect attempt to simplify a n	nixed num	ıber				
	eg $3\frac{3}{16} = 3\frac{1}{8}$			M1M1A1B1			
5 cont	$3\frac{3}{16}$ seen, then $\frac{51}{16}$ on answer line			M1M1A1B0			
	$\frac{9}{2}$ and $\frac{8}{3}$, $\frac{27}{6} \div \frac{16}{6}$,	<u>27</u> 16	, 1 <u>11</u> 16	M1M1A0B1ft			
	$\frac{9}{2}$ and $\frac{8}{3}$, $\frac{27}{6} \div \frac{16}{6}$,	1 <u>11</u> 16		M1M1A0B1ft			
	$\frac{9}{2}$ and $\frac{4}{3}$, $\frac{27}{6} \div \frac{8}{6}$,	$\frac{27}{8},$	$3\frac{3}{8}$	M0M1A0B1ft			

Question	Ar	nswer	Mark	Comme	nts
	Alternative me	thod 1			
	Correct reading value	of at least one		may be seen on graph	
	at 0 hours	[46, 50]			
	at 1 hour	[63, 67]	M1		
	at 2 hours	[80, 84]			
	at 3 hours	[96, 100]			
	at 4 hours	[114, 118]			
	subtraction of two	o values of hours	M1	division by 1 may be in	nplied
	17		A1	SC1 29	
	Alternative method 2				
	A difference in t	he range		may be seen on graph	
6	for 1 hour	[15, 19]			
	for 2 hours	[32, 36]	M1		
	for 3 hours	[49, 53]			
	for 4 hours	[66, 70]			
	difference correct number o	fhours	M1	division by 1 may be in	nplied
	17		A1	SC1 29	
	Additional Guidance				
	(119 – 42) ÷ 4 = 19.25				M0M1A0
	for 2nd M1 in Al recovered	t 1, subtraction must t	be in the c	orrect order unless	
	17 does not imply three marks, so working must be checked eg $(110 - 42) \div 4 = 17$			M0M1A0	

Question	Answer	Mark	Comments
	Alternative method 1		
	(5 – 2) × 180 or 3 × 180 or 540 or 180 – (360 ÷ 5) or (180 – 72) or 108	M1	oe
	Ticks 'No' and 540 or Ticks 'No' and 108	A1	
	Alternative method 2		
7	States that a pentagon cannot have five (or all) right angles or states that a pentagon can have five (or all) obtuse angles or states that the maximum number of right angles is three or draws a pentagon with exactly three right angles shown	M1	
	Ticks 'No' and states that a pentagon cannot have five (or all) right angles or states that the maximum number of right angles is three or states that a pentagon can have five (or all) obtuse angles and draws a correct diagram of an attempted pentagon with four right angles shown or draws a pentagon with exactly three right angles shown or draws a pentagon with five obtuse angles	A1	

The Additional Guidance for question 7 is on the next page

Question	Answer	Mark	Commer	nts	
Additional Guidance					
7	If comparing 72° to 90°, they must state that they are referring to the exterior angles				
cont If 'Yes' is ticked, M1 can still be scored					
	If neither box is ticked, 'No' must be in M1A1				

	8 and lowest (value)		oe	
	or	B1	Accept 102 for day 8	
	8 and outlier			
	Ade	ditional Gu	idance	
	8 and '(Only 102 landed whereas) All	the other o	lays were over 140'	B1
	8 and 'Fewer (less) planes landed (th	an the othe	er days)'	B1
	8 and 'It's an anomaly'			B1
	8 and 'There was a (big) drop / reduc planes'	ase in the number of	B1	
	8 and 'There were only 102 planes'			B1
8(a)	8 and 'It's low' or 8 and 'It's lower' of	B1		
	8 and 'It doesn't follow the trend (or p	B1		
	8 and 'It reduces a lot that day'			B1
	Ignore a non-contradictory statement with a correct statement			
	eg 8 and It's the lowest, it dropped by 53'			B1
	Do not award B1 with a numerical err	or in the st	atement	
	eg 8 and 'It's the lowest by 40'			B0
	8 and 'There were 102 planes'			B0
	8 and 'There's a drop of 53 (implies a	point to po	bint comparison)'	B0
	8 and 'It's below average'			B0
	8 and 'It's the odd one out'			B0

Question	Answer	Mark	Comments		
	Alternative method 1				
	$150 \times 24 \div 4$ or 150×6 or 900	M1	0e		
	their 900 × 365		for 365, allow 336, 360, 364, 366, 370		
	or		and 400		
	their 900 × 7 × 4 × 12	Malaia			
	or	мтаер			
	their 900 × 7 × 52				
	or 302400 or 360000				
	324000 or 327600 or 328500 or 329400 or 333000	A1			
	Alternative method 2				
8(b)	365 × 150 or 54750	N/1	for 365, allow 336, 360, 364, 366, 370 and 400		
	365 × any multiple of 150	IVIT	for 54750 allow 50400, 54000, 54600, 54900, 55500 and 60000		
	their 54750 × 24 ÷ 4 or 302400 or 360000	M1dep			
	324000 or 327600 or 328500 or 329400 or 333000	A1			
	Alternative method 3				
	365 × (24 ÷ 4) or 365 × 6 or 2190	N/1	for 365, allow 336, 360, 364, 366, 370 and 400		
-			for 2190, allow 2016, 2160, 2184, 2196, 2220 and 2400		
	their 2190 × 150 or 302 400 or 360 000	M1dep			
	324000 or 327600 or 328500 or 329400 or 333000	A1			

Question	Answer	Mark	Commer	nts	
8(c)	Ticks 'Her prediction could be too low or too high' and explains that fewer landings in winter would make it too low, but fewer landings at night would make it too high or states that the actual numbers are not given	B2	oe reason B1 ticks 'Her prediction cou too high'	ld be too low or	
	Additional Guidance				
	Ticks 'Her prediction could be too low or too hi is not enough data		gh' and states that there	B1 only	

Question	Answer	Mark	Commer	nts
	Alternative method 1			
	$(6^2 =) 36 \text{ or } (8^2 =) 64$ or 100 or $\sqrt{100}$	M1		
	10	A1		
	their $10 = 5a$ or (their $10)^3 = 125a^3$ or $1000 = 125a^3$ or $8 = a^3$	M1		
	2	A1ft	ft their 10 with both meth	nod marks scored
	Alternative method 2			
9	5 or <i>a</i>	M1		
	5 <i>a</i>	A1		
	their $5a = \sqrt{100}$ or their $5a = 10$	M1	$(a =) \frac{\sqrt{100}}{5}$ or $(a =) \frac{10}{5}$	implies M1A1M1
	2	A1ft	ft their $5a$ with both meth	nod marks scored
	Additional Guidance			
	Use the scheme that gives the better mark			
	eg1 $\sqrt{14^2} = 5a$, 14 = 5a, a = 2.8 scores M0A0M1A0 on alt 1 and M1A1M0A0 on alt 2			Award M1A1M0A0
	eg2 $\sqrt{100} = 5a^3$, $10 = 5a^3$, $a = \sqrt[3]{2}$ M1A0M1A1ft on alt 2	scores M1	A1M0A0 on alt 1 and	Award M1A0M1A1ft

Question	Answer	Mark	Comments	
	Alternative method 1			
	Alternative method 1			
	280 – 80 or 200	M1		
	their 200 ÷ 80 (× 100) or 2.5 (× 100)	M1dep	oe	
	250	A1		
	Alternative method 2			
10	280 ÷ 80 or 3.5	M1	oe	
	280 ÷ 80 × 100 (- 100) or their 3.5 × 100 (- 100) or 350 (- 100) or (their 3.5 - 1) (× 100)	M1dep	oe	
	or 2.5 (× 100)			
	250	A1		
11	A and D	B1		

Question	Answer	Mark	Commer	nts
	Alternative method 1			
	(x+a)(x+b)	M1	where $ab = \pm 12$ or $a + b =$	= –1
	(x-4)(x+3)	A1		
	4 and –3	A1	SC1 4 or –3 with no or one inc	correct answer
	Alternative method 2			
	$\frac{()1 \pm \sqrt{((-)1)^2 - 4(1)(-12)}}{2(1)}$ or $\frac{1 \pm \sqrt{1 + 48}}{2}$ or $\frac{1 \pm \sqrt{49}}{2}$	M1	oe allow one sign error	
	$\frac{2}{()1 \pm \sqrt{((-)1)^2 - 4(1)(-12)}}$ or $\frac{1 \pm \sqrt{1 + 48}}{2}$ or $\frac{1 \pm \sqrt{49}}{2}$	A1	oe fully correct	
12	4 and –3	A1	SC1 4 or –3 with no or one inc	correct answer
	Alternative method 3			
	$\left(x-\frac{1}{2}\right)^2$	M1		
	$\left(x-\frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^2 - 12 (= 0)$	A1	oe equation	
	4 and –3	A1	SC1 4 or –3 with no or one inc	correct answer
	Ade	ditional G	uidance	
	4 and –3 with no working			M1A1A1
	M1 can be scored amongst incorrect	attempts to	o factorise	
	Condone trailing bracket missing eg	(x - 4)(x + 4)	- 3	M1A1

Question	Answer	Mark	Commer	its
	Alternative method 1			
	2 x 5 : 3 x 5 or 10 : 15 and 5 x 3 : 4 x 3 or 15 : 12	M1	oe common value for f eg 10:15:12 or $\frac{2}{3}$:	1 : 4 5
	10 : 12	M1dep	oe unsimplified ratio condone fractions or decimals	
	5:6	A1		
	Alternative method 2			
13	3e = 2f and $4f = 5g$	M1	oe equations	
	6e = 5g	M1dep	oe equation	
	5:6	A1		
	Additional Guidance			
	Variables in an otherwise correct answer: the same variable scores 2 marks, eg $5f: 6f$ different variables do not score, unless earlier marks can be awarded, eg $5e: 6g$ with no working worth M1 or M1M1			M1M1A0 M0M0A0

14	1 - 0.3 - 0.15 - 0.35 or $1 - 0.8$ or 0.2 or 0.15 + 0.35 (+ 0.2) or $0.5 (+ 0.2)or1 - 0.3or$	M1	oe		
14	A' U B clearly shaded on diagram				
	0.7	A1	oe fraction, decimal or pe	ercentage	
	Additional Guidance				
	Do not award M1 for 0.15 + 0.35 or 0. calculation				
	eg 0.15 + 0.35 = 0.5, 0.5 + 0.3 = 0.8 (no further working)			MO	

Question	Answer	Mark	Commer	nts	
	C and 'lowest median'	B2	oe		
			B1 C		
	Additional Guidance				
	If the value of the median is given it must be 4 for B2				
15(a)	Accept midpoint oe for median				
	Do not accept mean for median				
	Only accept average for median if the				
	Accept mention of the lowest lower quartile with correct mention of the median for B2, but do not accept mention of any extra statistical measure as part of their justification				

	B and 'lowest interquartile range' or B and 'lowest range'	B2	oe B1 B		
	Additional Guidance				
15(b)	If the value of the interquartile range i If the value of the range is given it mu				
	For B2, do not accept non-statistical reasons, eg 'the narrowest box'				
	For B2, do not accept mention of any their justification				

Question	Answer	Mark	Comme	nts	
16	27 000	B1			
	$\left(\frac{4}{3}\right)^3 \text{ or } \frac{4^3}{3^3} \text{ or } \left(\frac{27}{64}\right)^{-1} \text{ or } \frac{1}{\frac{27}{64}}$ $\text{ or } \frac{1}{\left(\frac{3}{4}\right)^3} \text{ or } \frac{1}{0.75^3} \text{ or } \left(\frac{1}{0.75}\right)^3$	M1			
17	$\frac{64}{27}$ or $2\frac{10}{27}$	A1	oe fraction, mixed numbe	r or decimal	
	Additional Guidance				
	$\frac{64}{27}$ followed by an incorrect attempt to convert to a mixed number			M1A1	
	27 64			M0A0	

Question	Answer	Mark	Commer	nts	
	Alternative method 1				
	$\frac{1}{4}$ (completed) or $\frac{3}{4}$ (left)	M1	oe eg 25% (completed) or	75% (left)	
	$\frac{1}{8} + \frac{1}{10}$ or $\frac{9}{40}$	M1	oe eg 12.5% + 10% or 22	.5%	
	$\frac{3}{4}$ ÷ their $\frac{9}{40}$	M1dep	oe eg 75% ÷ their 22.5% dep on M1M1		
	$3\frac{1}{3}$ or 4 days with correct working seen	A1	oe		
	Alternative method 2 – assumes a number of nages (eq 80)				
	$\frac{3}{4}$ × their 80 or 60	M1	0e		
18	$\frac{1}{8}$ × their 80 or 10 and $\frac{1}{10}$ × their 80 or 8	M1	oe		
	their 60 ÷ (their 10 + their 8)	M1dep	oe dep on M1M1		
	$3\frac{1}{3}$ or 4 days with correct working seen	A1	oe		
	Additional Guidance				
	8 - 2 = 6, $10 - 6 = 4$, answer 4			MOMOMOAO	
	In alt 1, for the third mark allow a build-up method in percentages, fractions or decimals showing that 3 days is not enough (and 4 is enough)				
	eg 47.5%, 70%, 92.5%, (115%), answer 4			M1M1M1A1	

Question	Answer	Mark	Commer	nts
40(-)	2(x+5) = y+8	N/1	oe eq $\frac{x+5}{x+5} = \frac{1}{x+5}$ or	$\frac{y+8}{2} = 2$
	or $2x + 10 = y + 8$		y + 8 = 2	<i>x</i> +5 - 2
19(a)	2x + 10 = y + 8			
	and $y = 2x + 2$	A1		
		· ·		
	x + 10 = y + 1	M1	oe	
	Eliminates x or y from	M1	their (x + 10) = y + 1 mu	st be an equation
	their $(x + 10) = y + 1$		in x and y	
	and $y = 2x + 2$		eg	
	-		x + 10 = y - 1 (and $y = 2$	2x + 2)
19(b)			followed by	
			x + 11 = 2x + 2	
	x = 7 and $y = 16$	A1		
	Additional Guidance			
	x = 7 or $y = 16$ with no value or an incorrect value for the other unknown and no working worth M marks			MOMOAO

Question	Answer	Mark	Comments
	Alternative method 1		
	angle QPR = 27	M1	may be seen on diagram
	angle <i>XPS</i> = $\frac{180 - 50}{2}$ or 65	M1	may be seen on diagram
	angle QPR = 27		
	and		
	angle XPS = 65	A1	
	and		
20	angle QPS = 92		
	and		
	angle in a semicircle is a right angle		oe accept 92 ≠ 90
	all reasons for angle facts:		
	angles in same segment (are equal)		oe
	and	Δ1	
	angle sum of triangle (is 180)		oe
	and		
	base angles of isosceles triangle (are equal)		Oe

Question	Answer	Mark	Comments
	Alternative method 2	1	
	angle <i>SXR</i> = 180 – 50 or 130 and		may be seen on diagram
	angle <i>XRS</i> = 180 – their 130 – 27 and	M1	angle XRS = 23
	angle PQS = their 23		
	angle $XSP = \frac{180 - 50}{2}$ or 65	M1	may be seen on diagram
	angle SXR = 130		
	and		
	angle XRS = 23		
	and		
	angle <i>P</i> QS = 23	A1	
	and		
20 cont	<i>XSP</i> = 65		
	and		
	angle QPS = 92		
	and		
	angle in a semicircle is a right angle		oe accept 92 ≠ 90
	all reasons for angle facts:		
	angles on a straight line (add up to		oe
	180)		
	and		
	angle sum of triangle (is 180)	۸1	oe
	and	A1	
	angles in same segment (are equal)		oe
	and		
	base angles of isosceles triangle (are equal)		oe

Question	Answer	Mark	Comments	
	Alternative method 1			
	(second differences =) 4 or $2n^2$ or $a = 2$	M1	second difference seen at least once and not contradicted	
	11 - 2 × 1 ² and 26 - 2 × 2 ² and 45 - 2 × 3 ² (and 68 - 2 × 4 ²) or 9 and 18 and 27 (and 36) or 9 <i>n</i>	M1dep		
	$2n^2 + 9n$	A1	ое	
	Alternative method 2			
21	any two of a + b + c = 11 4a + 2b + c = 26 9a + 3b + c = 45 16a + 4b + c = 68	M1		
	3a + b = 26 - 11 and $5a + b = 45 - 26$ or a = 2 and $b = 9$ (and $c = 0$)	M1dep	oe obtains two correct equations in same two variables from their equations	
	$2n^2 + 9n$	A1	ое	
	Alternative method 3			
	(second differences =) 4 or $2n^2$ or $a = 2$	M1	second difference seen at least once and not contradicted	
	3a + b = 26 - 11 and substitutes $a = 2$ or $b = 9$ or $9n$	M1dep		
	$2n^2 + 9n$	A1	oe	

Question	Answer	Mark	Commer	nts
	Any two of $x(x-2)$ and $7(x + 4)$ and $(x-2)(x + 4)$	M1	oe x(x - 2) and $7(x + 4)$ can denominators	annot be
	correct equation including x(x-2) and $7(x + 4)and (x-2)(x + 4)$	M1dep		
	$x^2 - 2x + 7x + 28 = x^2 + 4x - 2x - 8$	M1dep	oe all brackets must be	expanded
	-12	A1		
22	Alternative method 2	1		
	$\frac{x(x-2)}{x+4} + 7 = x - 2$	M1		
	$\frac{x(x-2)}{x+4} = x - 9$ or $x(x-2) = (x-9)(x+4)$	M1dep		
	$x^{2} - 2x = x^{2} - 9x + 4x - 36$	M1dep	oe all brackets must be	expanded
	-12	A1		
	Alternative method 3	11		
	$x + \frac{7(x+4)}{x-2} = x + 4$	M1		
	$\frac{7(x+4)}{x-2} = 4$ or $7(x+4) = 4(x-2)$	M1dep		
	7x + 28 = 4x - 8	M1dep	oe all brackets must be	expanded
	-12	A1		
	Ad	ditional G	uidance	
	In Alt 1, do not allow $x \times x - 2$ or $7 \times x$	x + 4 unles	s recovered	

Question	Answer	Mark	Comments		
	Alternative method 1				
	$\sqrt{4}$: $\sqrt{9}$ or 2 : 3	M1	length A : length B		
	30 ÷ their 3 × their 2 or 20	M1dep	length A		
23	480 ÷ their 20 or 24	M1dep	area cross section A		
	their 24 ÷ 4 × 9	M1dep			
	54	A1			
	Alternative method 2				
	$\sqrt{4}: \sqrt{9} \text{ or } 2:3$	M1	length A : length B		
	$(\sqrt{4})^3 : (\sqrt{9})^3$ or 8:27	M1dep	volume A : volume B		
	480 ÷ their 8 × their 27 or 1620	M1dep	volume B		
	their 1620 ÷ 30	M1dep			
	54	A1			

Question	Answer	Mark	Commer	nts	
	Alternative method 1				
	$\frac{2\sqrt{6}}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}}$ or $\frac{\sqrt{3}}{\sqrt{10}} \times \frac{\sqrt{10}}{\sqrt{10}}$	M1			
	$\frac{2\sqrt{30}}{5}$ or $\frac{4\sqrt{30}}{10}$ or $\frac{\sqrt{30}}{10}$	M1dep			
	$\frac{3\sqrt{30}}{10}$	A1			
	Alternative method 2				
24	$\frac{2\sqrt{6}\sqrt{2}}{\sqrt{10}} - \frac{\sqrt{3}}{\sqrt{10}}$ or $\frac{2\sqrt{12}}{\sqrt{10}} - \frac{\sqrt{3}}{\sqrt{10}}$	M1	oe common denominato eg $\frac{2\sqrt{60}}{\sqrt{50}} - \frac{\sqrt{15}}{\sqrt{50}}$	r	
	$\frac{4\sqrt{3}}{\sqrt{10}} - \frac{\sqrt{3}}{\sqrt{10}}$ or $\frac{3\sqrt{3}}{\sqrt{10}}$	M1dep	oe common denominator and common surd in numerator $\frac{4\sqrt{15}}{\sqrt{50}} - \frac{\sqrt{15}}{\sqrt{50}} \text{ or } \frac{3\sqrt{15}}{\sqrt{50}}$		
	$\frac{3\sqrt{30}}{10}$	A1			
	Additional Guidance				
	Ignore an attempt at further simplification after $\frac{3\sqrt{30}}{10}$ M1			M1M1A1	

Question	Answer	Mark	Comments		
	Alternative method 1				
	$a(-3)^{2} + b(-3) + c = 0$ or $a(3)^{2} + b(3) + c = 0$	M1	ое		
	any two of (-)6 b = 0, c = 18 and 9 a + 18 = 0	M1dep	oe		
	$y = 18 - 2x^2$	A1	oe equation		
	Alternative method 2				
25	$y = 18 - 2x^2$	B3	oe equation B2 correct equation missing $y =$ eg $18 - 2x^2$ B1 equation of a quadratic curve that passes through (-3, 0) or (3, 0) or (0, 18) condone missing $y =$ eg $(y =) 18 - x^2$ or $(y =) (3 + x)(3 - x)$ or $(y =) x^2 - 2x - 3$ or $(y =) (x + 3)(x - 3)$		
	Additional Guidance				
	Correct equations include y = 2(3 + x)(3 - x) y = -2(x + 3)(x - 3) y = (6 + 2x)(3 - x) y = (3 + x)(6 - 2x)				
	For B3, B2 or B1 ignore incorrect expansion after correct equation or expression seen				

Question	Answer	Mark	Comments		
	Alternative method 1				
	$0.5 \times 20 \times x \times \sin 60$ or $10x \sin 60$ or $5\sqrt{3}x$	M1	Oe		
	$0.5 \times 20 \times x \times \sin 60 = 25\sqrt{3}$ or $x = 5$	M1dep	oe equation		
	(their 5) ² + 20 ² - 2 × their 5 × 20 × cos 60 or 25 + 400 - 200 cos 60 or 325	M1	oe their 5 must be their value of <i>x</i>		
	$\sqrt{\text{their } 325}$	M1dep	dep on 3rd M1 their 325 can be unsimplified		
	5 √13	A1			
26	Alternative method 2				
	$0.5 \times 20 \times h = 25\sqrt{3}$ or $h = \frac{5\sqrt{3}}{2}$	M1	oe any letter <i>h</i> is perpendicular height for 20 cm base		
	$\sin 60 = \frac{\text{their } \frac{5\sqrt{3}}{2}}{x}$ or x = 5	M1dep	oe		
	(their 5) ² + 20 ² - 2 × their 5 × 20 × cos 60 or 25 + 400 - 200 cos 60 or 325	M1	oe their 5 must be their value of <i>x</i>		
	$\sqrt{\text{their } 325}$	M1dep	dep on 3rd M1 their 325 can be unsimplified		
	5√13	A1			

Question	Answer	Mark	Commer	nts	
	Alternative method 3				
26 cont	$0.5 \times 20 \times h = 25\sqrt{3}$ or $h = \frac{5\sqrt{3}}{2}$	M1	oe any letter <i>h</i> is perpendicular height	t for 20 cm base	
	$\tan 60 = \frac{\text{their } h}{c}$ or $c = \frac{5}{2}$	M1dep	oe any letter <i>c</i> is part of 20 cm base		
	$\left(\text{their}\frac{5\sqrt{3}}{2}\right)^2 + \left(20 - \text{their}\frac{5}{2}\right)^2$ or $\left(\text{their}\frac{5\sqrt{3}}{2}\right)^2 + \left(\frac{35}{2}\right)^2 \text{ or } 325$	M1dep			
	$\sqrt{\left(\text{their } \frac{5\sqrt{3}}{2}\right)^2 + \left(20 - \text{their } \frac{5}{2}\right)^2}$ or $\sqrt{\text{their } 325}$	M1dep			
	5√13	A1			
	Additional Guidance				
	Omitting 0.5 in area formula can score a maximum of M0M0M1M1A0				
	$\sqrt{(\text{their 5})^2 + 20^2 - 2 \times \text{their 5} \times 20 \times \cos 60}$			M0M0M1M1A0	
27(a)	-k	B1			

27(b)	k	B1	