| Surname |
| :--- |
| Other Names |


| Centre <br> Number | Candidate <br> Number |
| :--- | :--- |
| 0 |  |

## GCSE <br> 3310U50-1 <br> <br> MATHEMATICS - NUMERACY <br> <br> MATHEMATICS - NUMERACY <br> <br> UNIT 1: NON-CALCULATOR <br> <br> UNIT 1: NON-CALCULATOR <br> <br> HIGHER TIER

 <br> <br> HIGHER TIER}
S18-3310U50-1

TUESDAY, 8 MAY 2018 - MORNING

1 hour 45 minutes

## ADDITIONAL MATERIALS

The use of a calculator is not permitted in this examination. A ruler, a protractor and a pair of compasses may be required.

## INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.
You may use a pencil for graphs and diagrams only.
Write your name, centre number and candidate number in the spaces at the top of this page.
Answer all the questions in the spaces provided.
If you run out of space, use the continuation page at the back of the booklet. Question numbers must be given for the work written on the continuation page.
Take $\pi$ as $3 \cdot 14$.

## INFORMATION FOR CANDIDATES

You should give details of your method of solution when appropriate.
Unless stated, diagrams are not drawn to scale.
Scale drawing solutions will not be acceptable where you are asked to calculate.
The number of marks is given in brackets at the end of each question or part-question.
In question 1(a), the assessment will take into account the quality of your linguistic and mathematical organisation, communication and accuracy in writing.

| For Examiner's use only |  |  |
| :---: | :---: | :---: |
| Question | Maximum <br> Mark | Mark <br> Awarded |
| 1. | 10 |  |
| 2. | 4 |  |
| 3. | 6 |  |
| 4. | 5 |  |
| 5. | 5 |  |
| 6. | 6 |  |
| 7. | 6 |  |
| 8. | 4 |  |
| 9. | 6 |  |
| 10. | 5 |  |
| 11. | 4 |  |
| 12. | 3 |  |
| 13. | 8 |  |
| 14. | 8 |  |
| Total | 80 |  |

## Formula List - Higher Tier

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=$ area of cross-section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


In any triangle $A B C$
Sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$
Area of triangle $=\frac{1}{2} a b \sin C$


## The Quadratic Equation

The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$ are given by $\quad x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

## Annual Equivalent Rate (AER)

AER, as a decimal, is calculated using the formula $\left(1+\frac{i}{n}\right)^{n}-1$, where $i$ is the nominal interest rate per annum as a decimal and $n$ is the number of compounding periods per annum.

## BLANK PAGE

## PLEASE DO NOT WRITE ON THIS PAGE

1. (a) In this part of the question, you will be assessed on the quality of your organisation, communication and accuracy in writing.

The concrete base of Miss Morgan's new bungalow is shown below.


Diagram not drawn to scale
The concrete base of Miss Morgan's bungalow is 0.2 m thick.


Calculate the volume of the concrete base.
You must show all your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


Olga took out a high-interest loan for $£ 400$.
She paid back $£ 49$ per month for 20 months to clear the loan.
Calculate the total interest that Olga paid as a percentage of the original loan.

## BLANK PAGE

## PLEASE DO NOT WRITE ON THIS PAGE

3. Sara is carrying out a survey of the three villages, Cwm, Allthir and Gwyndir.

The diagram below shows the positions of the three villages.


Diagram not drawn to scale
(a) What is the bearing of Allthir from Gwyndir? Circle your answer.
$010^{\circ}$
$170^{\circ}$
$180^{\circ}$
$190^{\circ}$
$200^{\circ}$
(b) What is the bearing of Cwm from Allthir?

Circle your answer.
$028^{\circ}$
$152^{\circ}$
$242^{\circ}$
$332^{\circ}$
$352^{\circ}$
(c) The area of the land covered by the three villages is $200 \mathrm{~km}^{2}$.

Examiner The total population of the three villages is 8400 people.
(i) What is the population density of the three villages?

Give your answer in population/km².
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(ii) The populations of Cwm , Althir and Gwyndir are in the ratio $3: 4: 5$. Calculate the population of Gwyndir.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
4. (a) Kingsley invests $£ 3000$ in an account that pays $2 \%$ compound interest per annum. He does not make any further payments into his account. He does not withdraw any money from his account.

How much will Kingsley have in his account after two years?

Amount in Kingsley's account after two years is $£$
(b) Kingsley buys a portable Bluetooth speaker.

The speaker has been reduced by $20 \%$ in a sale.
He pays $£ 72$ for the speaker in the sale.
What was the original price of the speaker?

Original price of the speaker is $£$
5. Michelle owns a café.

She stacks coffee mugs as shown in the diagram below.
Michelle measures the height of each coffee mug as 12 cm , correct to the nearest centimetre. Each stacked coffee mug creates 4 cm extra height, correct to the nearest centimetre.


## Diagram not drawn to scale

Michelle knows that the vertical height between two shelves is exactly 39 cm , as shown below.


Diagram not drawn to scale

Can Michelle be certain that she will be able to place one stack of 7 coffee mugs between the two shelves?
Give a reason for your answer.
You must show all your working.
6. This year, 50 runners took part in a 5 km race in the Brecon Beacons. All 50 runners finished the race.

The cumulative frequency diagram below shows the times taken by the runners to finish the race.

(a) Which is the modal group?

Circle your answer.
20 to 25 minutes 25 to 30 minutes 30 to 35 minutes
35 to 40 minutes $\quad 40$ to 45 minutes
(b) Is it certain that the last runner's finish time was 45 minutes?

You must give a reason for your answer.
Examiner

(c) The organisers hoped that $80 \%$ of the runners would finish the race within 30 minutes.

Complete the following two statements.

- $\qquad$ \% of runners finished the race within 30 minutes.'
' $80 \%$ of runners finished the race within minutes.'
(d) Last year, the median finish time was 26 minutes.

By how many minutes was the median time better this year?
You must show all your working.
7. There are two entrances to a stadium, North Entrance and South Entrance. At each entrance, 3000 people queued to pass through security.
The length of time each of these people spent in the queue was recorded. The box-and-whisker diagrams show the results.


(a) At the North Entrance, how many people had to queue for more than 44 minutes? You must show all your working.
(b) For the South Entrance, calculate an estimate of the number of people who had to queue there for between 40 and 60 minutes.
You must show all your working.

Number of people is
(c) At which entrance did the security team seem to be more effective at getting people into the stadium quickly?
You must give a reason for your answer.
North Entrance $\square$

South Entrance
$\square$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
8. Eirlys works for an accountancy firm. She receives an annual salary, which is paid in equal instalments.

Eirlys has calculated that, so far this financial year, she has been paid $0.41 \dot{6}$ of her annual salary.
(a) Express $0.41 \dot{6}$ as a fraction in its lowest terms.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) Use your answer from part (a) to find the number of months' pay Eirlys has received. [1]
9. Matas knows the following information about the amount of fuel his car uses.

| Speed | Miles per gallon |
| :---: | :---: |
| 30 mph | 54 |
| 50 mph | 60 |
| 70 mph | 50 |

During one journey, Matas drove at 50 mph for part of the time and at 70 mph for the rest of the time.
He drove for 3 hours at a speed of 50 mph .
For the whole journey, Matas used $4 \cdot 6$ gallons of fuel.
For how long did Matas travel at 70 mph ?
You must show all your working.
-
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\square$
10. Astronomers use astronomical units (AU) to describe distances in our solar system. The distance between the Sun and the Earth is 1 AU.
1 AU is $1.496 \times 10^{8} \mathrm{~km}$, correct to 4 significant figures.
(a) The distance of Pluto from the Sun is $5.913 \times 10^{9} \mathrm{~km}$, correct to 4 significant figures.


Siôn says that the distance of Pluto from the Sun is less than 50 AU .
Using suitable approximations, estimate the distance of Pluto from the Sun, in AU, to show that Siôn is correct.
You must show all your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) A light year is the distance light travels in one year.

1 light year is approximately 63000 AU .
Estimate the length of a light year in km.
Give your answer in standard form.
$\qquad$
$\qquad$
$\qquad$
11. During a chemistry experiment, it was found that a particle lost $\frac{3}{4}$ of its mass every second. The initial mass of the particle was 160 mg .
(a) Calculate the mass of the particle after 4 seconds. Circle your answer.
$\begin{array}{llll}2.5 \mathrm{mg} & 0.15625 \mathrm{mg} & 40 \mathrm{mg} & 0.625 \mathrm{mg}\end{array} 0.875 \mathrm{mg}$
Circle your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) Write down a formula for the mass $m$, in milligrams, of the particle after $t$ seconds.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
12. Ffiol-Aur is a company that makes vases.

They make one of their vases in two mathematically similar sizes.


Diagrams not drawn to scale

A decorative glaze covers the surfaces of each vase.
The glaze covers an area of:

- $400 \mathrm{~cm}^{2}$ on the smaller vase,
- $3600 \mathrm{~cm}^{2}$ on the larger vase.

The height of the larger vase is 48 cm .
Calculate the height of the smaller vase.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
13. The heights of all the Year 11 girls at a school were measured. Nia has started to draw a histogram of the results.

Frequency density

(a) There were 24 girls in Year 11 whose heights were in the group $155<h \leqslant 160 \mathrm{~cm}$. Use this information to complete Nia's histogram.

| (b) | Nia has started to do some data analysis on the heights of the Year 11 girls. She has estimated the median and the upper quartile, as shown in the table below. |  |  |
| :---: | :---: | :---: | :---: |
|  | Lower quartile | Median | Upper quartile |
|  |  | 151.75 cm | 156.875 cm |

Use the histogram to calculate an estimate of the lower quartile of the heights of the Year 11 girls.
14. The diagram shows the simplified model of part of an engine.

It shows a belt which runs around three circular cogs.
The engine rotates Cog 1.
Cog 1 rotates the belt, which then makes Cogs 2 and 3 rotate.


Diagram not drawn to scale
$A B, C D$ and $E F$ are straight sections of the belt.
$A B=12 \mathrm{~cm}, C D=34 \mathrm{~cm}$ and $E F=29 \mathrm{~cm}$.
The belt bends around the outer edges of the circular cogs, represented by the arcs $B C, D E$ and $A F$.
The dimensions of the cogs are:

- radius of $\operatorname{Cog} 1=6 \mathrm{~cm}$
- radius of $\operatorname{Cog} 2=4.5 \mathrm{~cm}$
- radius of $\operatorname{Cog} 3=3 \mathrm{~cm}$
(a) What is the length of arc $A F$ in terms of $\pi$ ?

Circle your answer.
$2 \pi$
$3 \pi$
$6 \pi$
$4 \pi$
$\frac{3 \pi}{2}$


Give your answer in terms of $\pi$ in its simplest form.
[4]

Calculate the number of revolutions Cog 2 will make in one minute.


Examiner only

